

Computational Aeroelasticity with CFD Models: Required Tools

Luca Cavagna

Dipartimento di Ingegneria Aerospaziale, Politecnico di Milano

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FOI Swedish Defence Agency, Kista - Stockholm



Outline

- 1 Motivations and targets
- 2 NAEMO-CFD: Computational Aeroelasticity for aircrafts
- 3 Spatial Coupling Method
 - Introduction to spatial coupling
 - Adopted Spatial Technique
- 4 Grid motion techniques
 - Introduction to grid motion
 - Adopted methods
 - Control surfaces deflection
- 5 Conclusions and developments

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Motivations and Targets

Why adopting CFD Models in Computational Aeroelasticity (CA)

- Enhance the modelling of the aerodynamics with non-linear effects
- Overcome the lacks provided by classic linear(ized) theories

Applications:

- Phenomena related to compressibility (Transonic Dip)
- Phenomena related to viscosity (separations, stall flutter, buffeting)
- Investigate Limit Cycle Oscillations (LCO)
- Consider interference effects (under-wing stores, innovative configurations, joined wings)

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Motivations and Targets

Few considerations

- **Apply Computational Aeroelasticity (CA) CFD in real life applications**
 - **Unsteady** CFD is now a research succesfull research field
 - **Computational costs** precluded it so far from extensive industrial applications
 - Aircraft is designed by different dedicated **departments**
 - **Large number** of configuration needs to be assessed

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Times are mature to apply fast CA in real industrial applications

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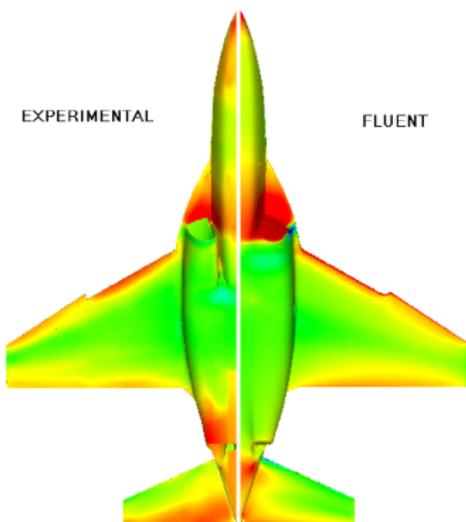
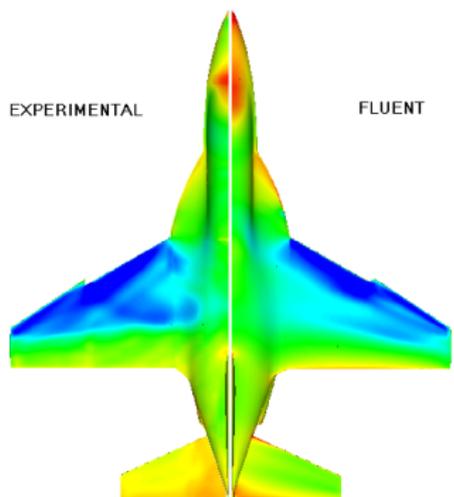
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NAEMO: Numerical AeroElastic MOdeller based on CFD models



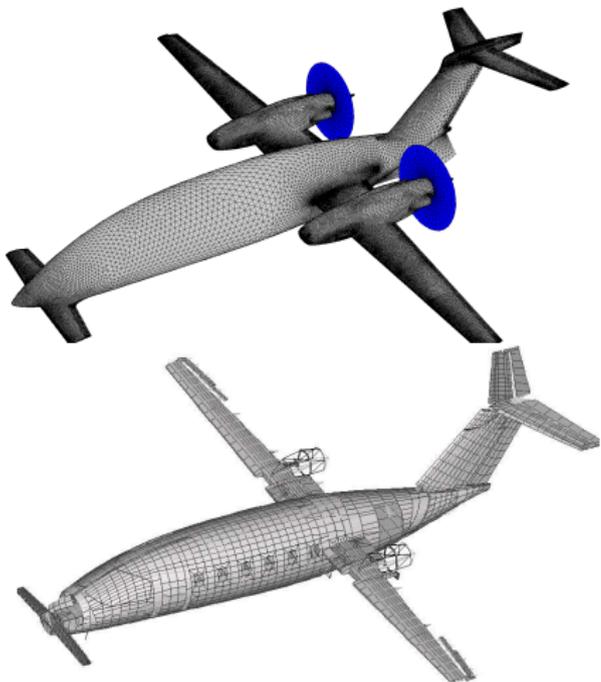
Aerodynamic model qualification

- RANS comparison to wind tunnel data
- Prediction of shock waves position

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Partitioned analysis issues



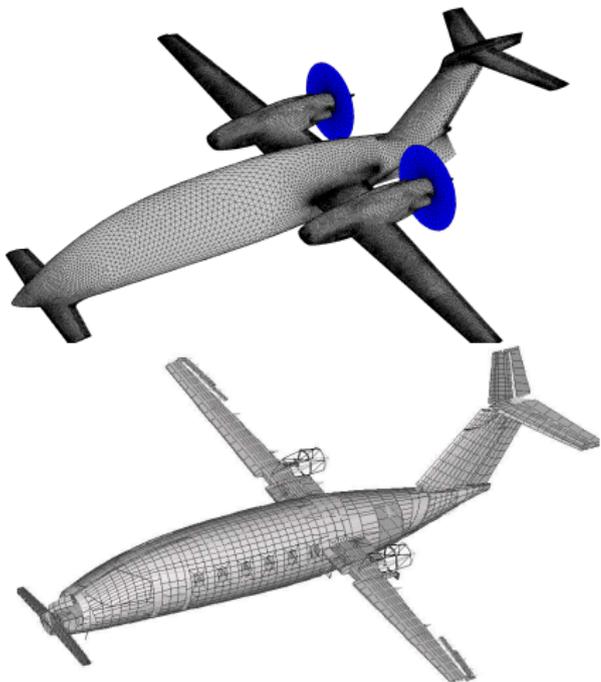
Modelling differences

- Discretizations
- Refinement
- Topologies
- Element formulation

Constraints

- Interpolation
- Extrapolation
- Mesh independence
- Conservation
- Localization

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Moving Least Square Technique (MLS): definition

Features

- **Meshless** approach
- Energy **conservation**
- Suitable for **complex** geometries and **incompatible** meshes
- Freedom to **rule** the quality/smoothness of the interpolation

Problem formulation

Reconstruction of a generic function $f \in C^d(\Omega)$, on a compact space $\Omega \subseteq \mathbb{R}^n$, from its values $f(\bar{\mathbf{x}}_1), \dots, f(\bar{\mathbf{x}}_N)$ on scattered distinct centres $X = \{\bar{\mathbf{x}}_1, \dots, \bar{\mathbf{x}}_N\}$

Note

It is not necessary to derive an analytical expression for f

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Moving Least Square Technique (MLS): conservation

Conservation issues

- Coupling conditions are enforced in a **weak** sense through a **variational** principle

Application of the Virtual Works Principle

Given two admissible virtual displacements $\delta \mathbf{y}_f$, $\delta \mathbf{y}_s$ for each field and matrix \mathbf{H}

$$\delta \mathbf{y}_f = \mathbf{H} \delta \mathbf{y}_s; \mathbf{F}_f = \mathbf{H} \mathbf{F}_s$$

then by equating the virtual works $\mathbf{W}_f, \mathbf{W}_s$:

$$\mathbf{W}_f = \delta \mathbf{y}_f^T \mathbf{F}_f = \delta \mathbf{y}_s^T \mathbf{H}^T \mathbf{F}_f = \delta \mathbf{y}_s^T \mathbf{F}_s$$

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Moving Least Square Technique (MLS): approximation

Local approximation

f is usually expressed as sum of monomial basis functions $p_i(\mathbf{x})$

$$\hat{f}(\mathbf{x}) = \sum_{i=1}^m p_i(\mathbf{x}) a_i(\mathbf{x}) \equiv \mathbf{p}^T(\mathbf{x}) \mathbf{a}(\mathbf{x}),$$

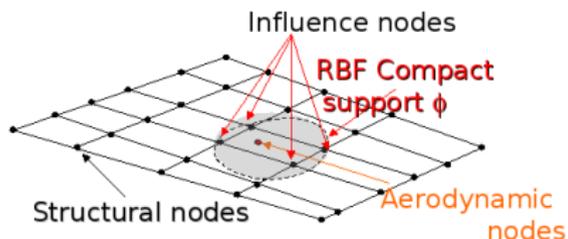
Interface matrix \mathbf{H} construction

The coefficients $\mathbf{a}_i(\mathbf{x})$ are obtained by performing a weighted least square fit for the approximation \hat{f}

$$\text{Minimise } J(\mathbf{x}) = \int_{\Omega} \phi(\mathbf{x} - \bar{\mathbf{x}}) \left(\hat{f}(\mathbf{x}, \bar{\mathbf{x}}) - f(\bar{\mathbf{x}}) \right)^2 d\Omega(\bar{\mathbf{x}}),$$

with the constraint: $\hat{f}(\mathbf{x}, \bar{\mathbf{x}}) = \sum_{i=1}^m p_i(\bar{\mathbf{x}}) a_i(\mathbf{x})$

Moving Least Square Technique (MLS): localization



Problem localization

Function W can be chosen as a smooth non-negative compact support Radial Basis Function

Wendland Radial Basis Functions (RBF)

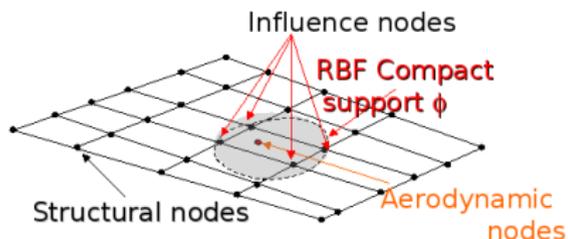
Usually written as function of (r/δ) , where δ is the support size
Example:

- $W(r/\delta) = (1 - r/\delta)^2 \quad (C^0 \text{ Wendland Function})$

User control

The smoothness is ruled by changing the support size δ and the number of source points through optimized searching algorithms

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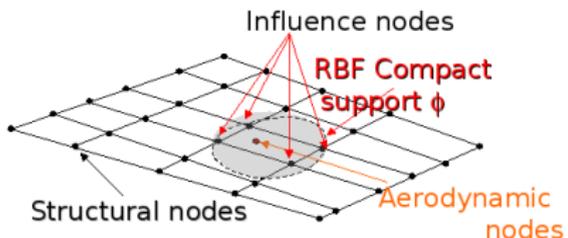
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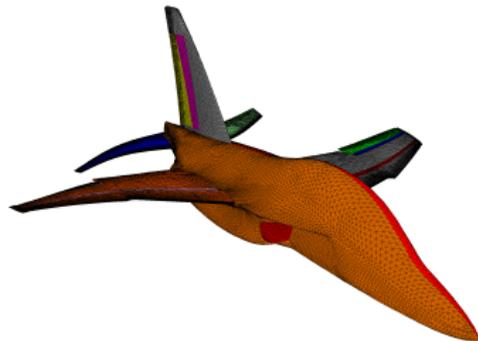
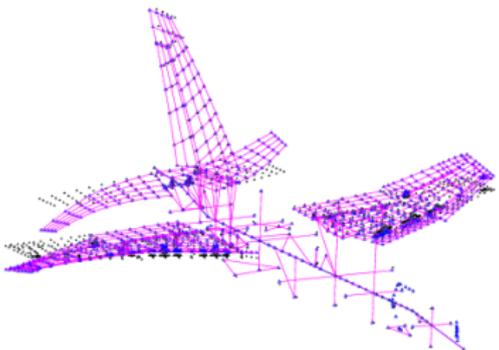
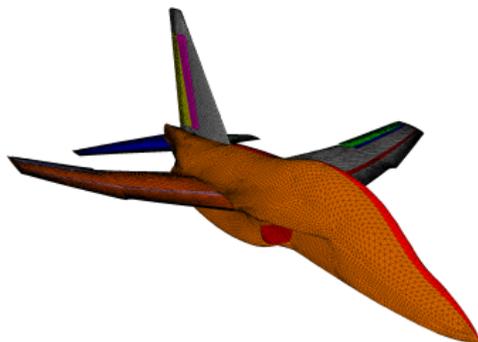
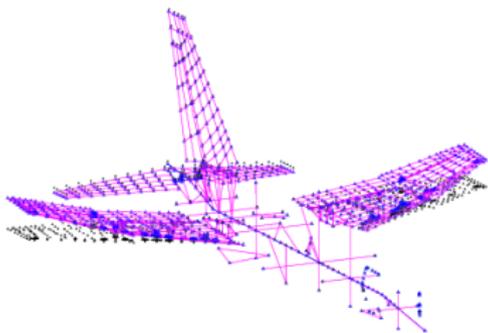
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Adopted Spatial Technique

Moving Least Square Technique (MLS): results



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Grid Motion: overview

Target

- Account for structural motion in a **general** way
- Avoiding complex methods like CHIMERA or re-meshing

Issues

- **Troublesome** (negative volumes, element distortions)
- **Time-consuming** (several thousands of cells, parallelization)
- Correct management of sliding/fixed nodes

Note

- No physical accuracy is required to solve this problem
- Several methods are thus based on structural analogies

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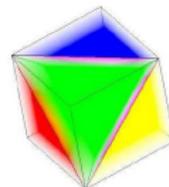
Grid Motion: continuum analogy method

Features

- CFD mesh is translated into an **FEM** continuum model
- Moving boundaries nodes contribute to system rhs
- Sliding nodes along generally oriented planes easily accounted
- Avoid **expensive** torsional springs (no rotational dof required)
- Cell **distorsions** are **automatically prevented**
- **Non-linearity** can be introduced if stiffness matrix is updated

Assumption

- Every element can be split into basic tetrahedra
- No gaussian quadrature is required



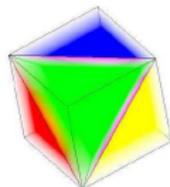
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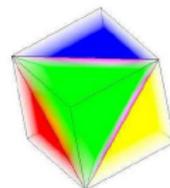
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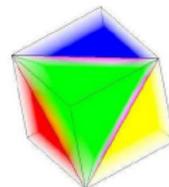
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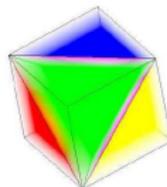
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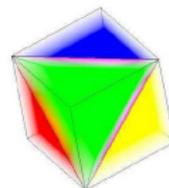
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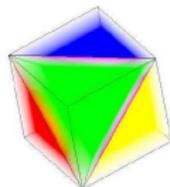
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Grid Motion: continuum analogy method

Negative volumes preventing

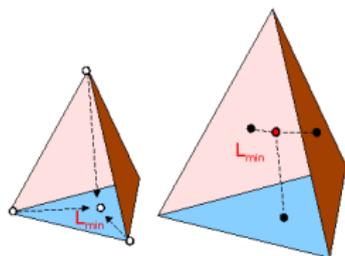
- Large cells far from moving faces are intentionally softened
- Each cell has a local *Young* modulus \mathbf{E} :

$$E_{el} = \frac{1}{\min_{j,k \in el} \|x_j - x_k\|^\beta}, \quad \nu \in [0.3 : 0.45]$$

- Additional stiffness introduced according to wall distance

Characteristic length choice

A well chosen length further prevents cell-collapsing



Grid Motion: continuum analogy method

Negative volumes preventing

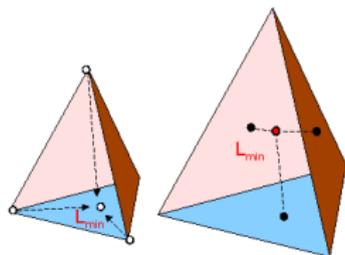
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Grid Motion: solution method

Solver

- Simple *smoothers* adopted (Jacobi, SOR)
- High frequency error is rapidly lowered
- Easy parallelization (good scalability)
- Each node deforms its CFD partitions
- Interface data exchanged

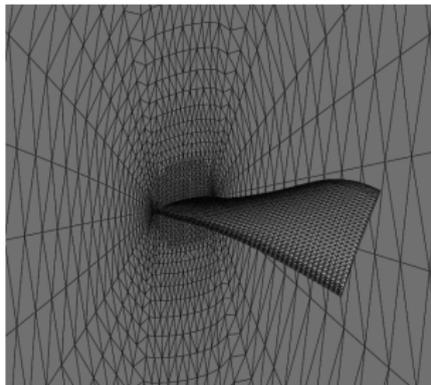
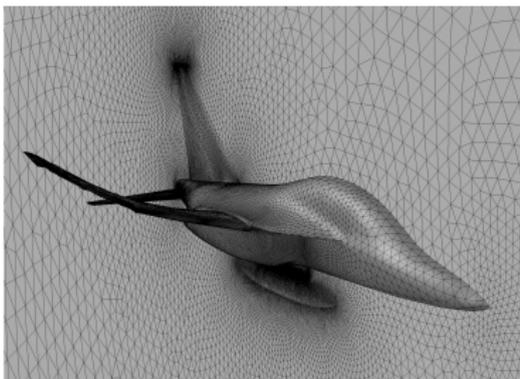
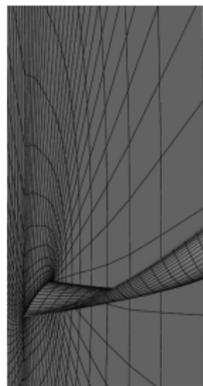
Negative volumes preventing

Displacement field can be subdivided into multiple tasks and stiffness updated



Grid Motion: results

Different results on structured and unstructured mixed grids



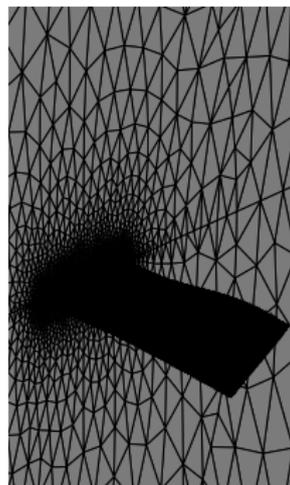
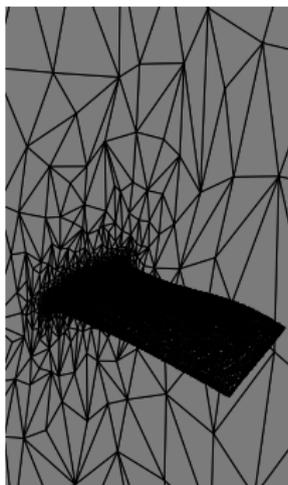
Grid Motion: further methods

Simplified strategies

- Store perturbation grids
- Thermal solver (three 1D runs)

Multigrid method

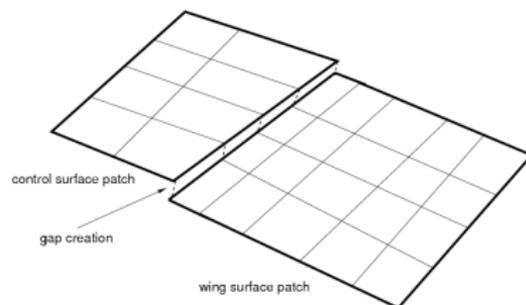
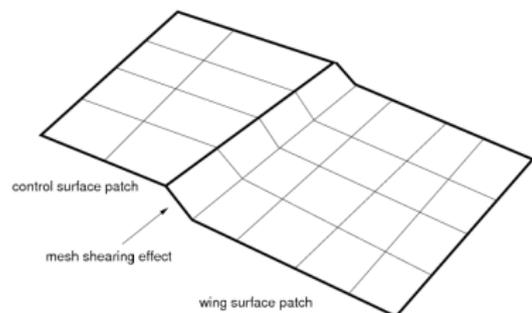
- A valid coarse grid is created
- Coarse deformation
- MLS interpolation for discarded nodes



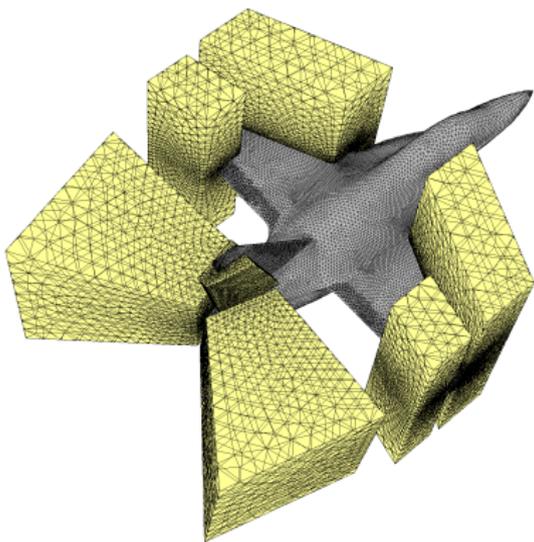
Grid Motion: control surfaces

Issues

- Control surfaces rotations locally lead to large displacements
- Gaps are created when a surface is deflected
- Gap meshing is not trivial and raise cell number
- Mesh shearing easiliy leads to ill-conditioned cells



Grid Motion: control surfaces deflection strategy



Adopted method

- Non-conformal mesh
- Sliding interfaces
- Fluxes calculation on intersecting faces
- Moving or fixed boxes

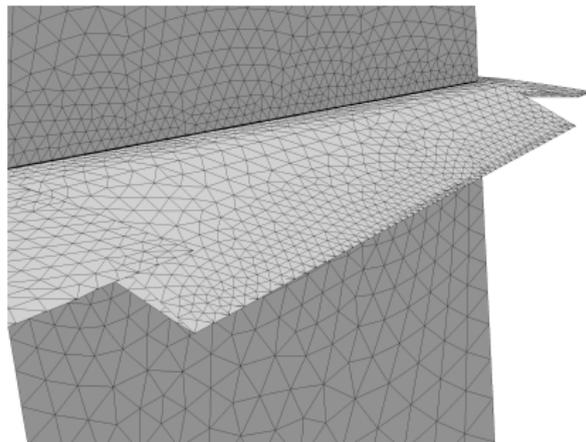
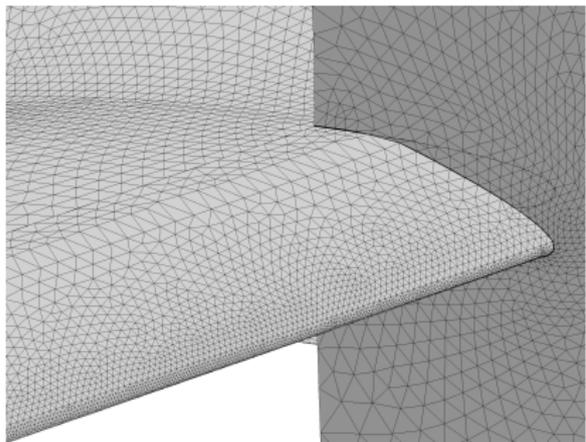
Note

Each box independently meshed and substituted if local refinement required

Grid Motion: control surfaces deflection strategy

Gap modelling

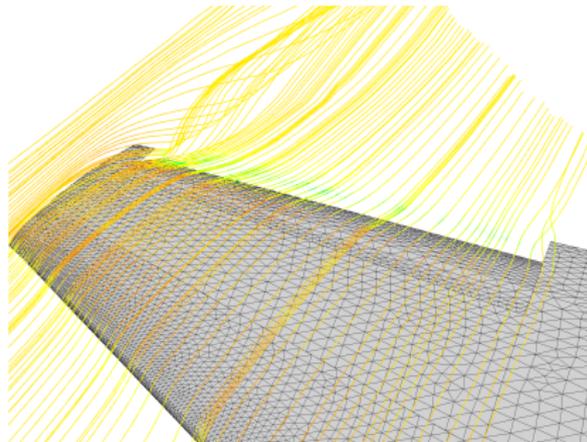
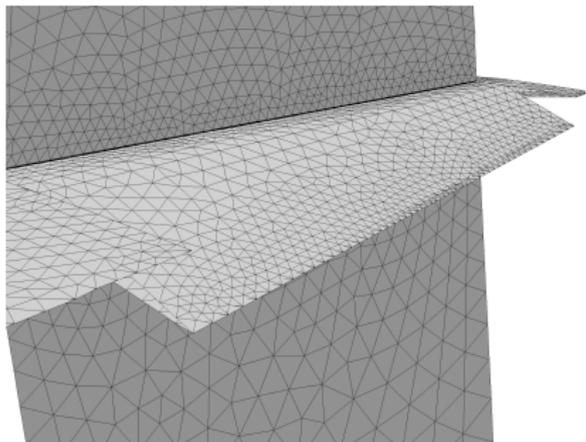
If one of the interface zones extends beyond the other, additional wall zones for the portion(s) of the non-overlapping boundary are created



Grid Motion: control surfaces deflection strategy

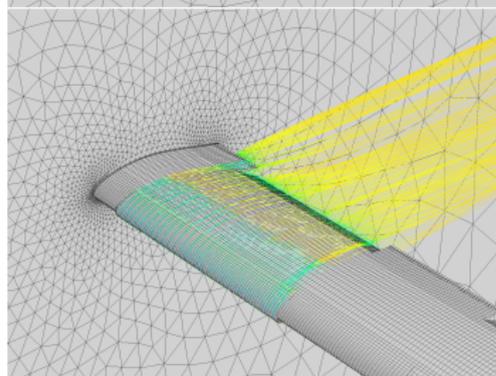
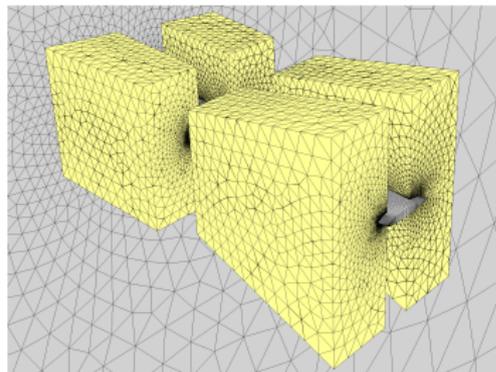
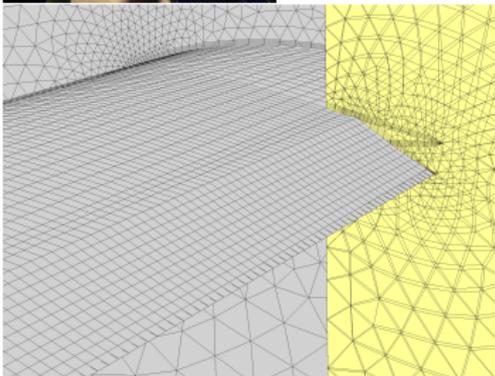
Gap modelling

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Control surfaces deflection

Grid Motion: control application



Outline

- 1 Motivations and targets
- 2 NAEMO-CFD: Computational Aeroelasticity for aircrafts
- 3 Spatial Coupling Method
 - Introduction to spatial coupling
 - Adopted Spatial Technique
- 4 Grid motion techniques
 - Introduction to grid motion
 - Adopted methods
 - Control surfaces deflection
- 5 Conclusions and developments

Conclusion and future developments

Conclusion

- Spatial coupling needs to be general for whatever model
- Conservation issues must be guaranteed
- Control on coupling smoothness and localization
- On line mesh deformation may be important
- Transpiration boundary condition can be exploited
- Control task is not trivial and requires dedicated techniques

Future developments

- Maneuvering deformable aircraft in transonic regime
- Coupling to Multibody dynamic solver MBDyn
(www.aero.polimi.it/~mbdyn)

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References



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